Understanding the role and interplay of heavy-hole and light-hole valence bands in the thermoelectric properties of PbSe

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The thermoelectric properties of PbSe have significantly improved in recent years reaching figures of merit \( ZT \sim 1.6 \). The transport properties of the hole-doped high temperature thermoelectric material PbSe are particularly interesting and play a key role in this. Here, they were analyzed over wide temperature and hole concentration ranges. The special features observed in the variation of the experimental Seebeck coefficient and Hall coefficient can be accounted for within the framework of a two-band model. Two valence bands separated by a temperature dependent energy offset are considered. The extremum of the light-hole band has a density of states mass \( \sim 0.27 \) \( m_0 \) at room temperature. It is nonparabolic and anisotropic and can be described by the Kane model. The extremum of the heavy-hole band is isotropic and parabolic with a much larger density of states mass \( \sim 2.5 \) \( m_0 \). We find that for heavily doped compositions, the high mass band contributes the Seebeck coefficient, even at room temperature. With rising temperature, holes are transferred from the light-hole to the heavy-hole branch, giving rise to the anomalous temperature dependent Hall coefficient, which is found peaked near \( \sim 650 \) K.

For Na-doped samples \( \text{Pb}_{1-x}\text{Na}_x\text{Se} \) for \( 0.01 \leq x \leq 0.03 \), the high thermopower values of \( 200 \sim 300 \mu \text{V/} \text{K} \) at 900 K arise from the heavy-hole band, which are responsible for the excellent thermoelectric performance of PbSe.

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I. INTRODUCTION

The high thermoelectric performance (\( ZT \)) of a semiconductor demands high thermoelectric power to produce maximum voltage in the circuit, large electrical conductivity to minimize losses due to Joule heating, and low thermal conductivity to retain maximum heat for conversion at the hot junction and avoid losses down the limbs to the cold sink [1]. The engineering of the electrical properties to achieve high power factor [2] and the reduction of the lattice component of the thermal conductivity through nanostructuring [3] are the main adopted strategies towards high thermoelectric performance in the case of lead chalcogenides.

The concept of band structure engineering stems from the complex valence band structure of Pb-chalcogenides, where two inequivalent maxima, the so-called light-hole band, and the lower lying heavy-hole band are located at the \( L \) and \( \Sigma \) points of the Brillouin zone, respectively, and the ability to control carrier access of these maxima with chemical or physical changes [4,5]. For example, the high effective hole mass of the \( \Sigma \) point band enhances the Seebeck coefficient if probed by heavy doping. Band structure engineering refers to alloying, on the other hand, of the Pb-chalcogenide matrix to achieve an effective tuning of the relative energies of the two bands [6–12]. Previously, extensive attention has focused on the analysis of the electrical transport properties of \( p \)-type PbTe, and the experimental results have been well interpreted in the framework of a two-band model; a low density of states (the light-hole band) and a high density of states (the heavy-hole band), which lies \( \sim 0.15 \) eV below in energy that contributes to the transport properties at high temperatures [5,13–18].

Lead selenide combines several attractive features relative to the tellurium analog, such as higher melting, lower cost, and higher operation temperatures. The well-known PbSe system [19–23] is now attracting considerable attention as a promising thermoelectric material for high temperature power generation applications. Heavily doped \( p \)-type PbSe has shown \( ZT \)s as high as \( \sim 1.2 \) at 850 K [24,25], while after the simultaneous improvement of both electrical and thermal properties, \( ZT \) values of \( \sim 1.4 \sim 1.6 \) can be obtained [9,12,25]. Theoretical calculations have suggested that hole-doped PbSe can potentially reach \( ZT \sim 2 \) at 1000 K [26], indicating prospects for further performance improvements. The common feature of the above studies is that high thermopower is achieved without any sign of saturation or turnover at high temperatures due to bipolar diffusion. It is believed that the high Seebeck coefficient originates from the complex band structure and the contribution of the high density of states heavy-hole band, lying deep in the valence band (much deeper than in PbTe). Under appropriate conditions of doping and temperature, this heavy-hole band may be exploited to enhance the thermoelectric performance of PbSe.

Based on the above, it is important to understand the electronic performance of PbSe over as broad a spectrum of carrier concentrations and as wide a temperature as possible. For this reason, we present here an in-depth study of the transport properties of heavily doped \( \text{Pb}_{1-x}\text{Na}_x\text{Se}, \) \( 0.01 \leq x \leq 0.03 \). We focus on the effects of doping and temperature, and we investigate the behavior of the complex valence band structure and its impact on the transport properties. Our experimental results included in our analysis cover a wide temperature range in this system. The Seebeck coefficient
and the electrical conductivity were measured in the range of 300–900 K, while the experimental Hall coefficient covers the temperature regime of 10–850 K.

This is a detailed application of a multiband model for PbSe over a broad temperature plateau. The experimental results are modeled by the adoption of two moving valence parts, a nonparabolic primary band and a parabolic secondary band, that cross each other at \( \sim 1500 \text{K} \). As a result, we can extract the partial transport properties of the two valence bands and their temperature dependence. Based on the Pisarenko plot, built with data from samples covering a wide range of doping compositions, we demonstrate that the heavy-hole band plays a role, even at room temperature. In particular, we show that for hole densities in the range of \( 2 \times 10^{20} \text{cm}^{-3} \), the Fermi level can cross the top of the heavy-hole band at room temperature. The analysis indicates that at high temperatures, holes from the light-hole band are transferred to the heavy-hole band, resulting in the anomalous temperature dependence of the Hall coefficient that it found peaked at 650 K. The heavy-hole band contributes the high Seebeck coefficient values above room temperature, and at 900 K, essentially the dominant contribution, accounting for the excellent thermoelectric performance of PbSe. The work described here explains previous qualitative interpretations of experimental findings and provides specific transport coefficients of the two valence bands for PbSe over the widest available temperature range.

A. Transport coefficients

Lead chalcogenides are multivalley narrow band-gap semiconductors with a direct gap at the \( L \) point of the Brillouin zone. Both the conduction and the valence bands are nonparabolic and anisotropic, showing multiple ellipsoidal constant-energy surfaces and two components of the effective mass [4,27]: the longitudinal \( m^*_L \), associated with the longitudinal axis of the ellipsoidal energy surfaces, and the transverse \( m^*_T \), associated with the two transverse axes of the surfaces. The different effective masses give rise to band anisotropy, defined as \( K = m^*_L/m^*_T \). Due to the nonparabolicity, the effective masses are functions of the energy \( \varepsilon \), defined by the interaction of electron and hole bands, the transport coefficients are described by the Kane model, and the density of states as a function of energy is given by [4,27]

\[
\rho(\varepsilon) = \frac{2^{3/2}m^*_L^{3/2}}{\pi^2\hbar^3} \varepsilon^{1/2} \left( 1 + \frac{\varepsilon}{E_g} \right)^{1/2} \left( 1 + \frac{2\varepsilon}{E_g} \right),
\]

where \( m^*_L = N^{2/3}(m^*_T m^*_H)^{2/3} \) is the total density of states mass, \( N \) is the number of the equivalent or degenerated valleys, and \( E_g \) is the \( L \) point fundamental gap. The relaxation time is inversely proportional to the density of states. Also, the mean-square matrix element of the interaction of a carrier with a scatterer decreases (due to the nonparabolicity) with increasing energy for acoustical and optical phonon scattering [4,27].

The mechanisms of charge carrier scattering in Pb-chalcogenides are both temperature and concentration dependent. For low temperatures, the scattering by the Coulomb and the short-range potential of vacancies are expected to dominate, while around or above room temperatures, the polarization scattering by optical phonons, the collision between carriers, the deformation potential of acoustic phonons, and the deformation potential of optical phonons are among the premier scattering mechanisms. Additionally, as a result of the complex band structure, the scattering of carriers between different valleys or bands is also expected to contribute [27–31]. Despite the complexity and the number of scattering mechanisms, the high temperature transport properties of heavily doped semiconductors may be described assuming the deformation potential of acoustic phonons as the dominant scattering mechanism, which is the case in the present paper. The deformation potential of acoustic phonons with that of optical phonons and the intervalley scattering actually produce an effective deformation potential coefficient [27,31]. For lead chalcogenides, the expression of the acoustic phonon relaxation time in the framework of the Kane model, after taking into account the energy dependent interaction matrix, is written [4,29,30,32]:

\[
\tau_{ac}(\varepsilon) = \tau_0(\varepsilon + \varepsilon^2\alpha)^{-1} \left[ 1 - \frac{8\alpha(\varepsilon + \varepsilon^2\alpha)}{3(1 + 2\varepsilon\alpha)^2} \right]^{-1}
\]

where \( \varepsilon = E/k_BT \) is the reduced energy and \( \alpha = k_B T/E_g \) is the band nonparabolicity parameter. At equilibrium, the carrier distribution follows the Fermi-Dirac statistics and is a function of the reduced energy and the reduced chemical potential \( \eta \) [27]:

\[
f(\varepsilon) = \frac{1}{1 + \exp(\varepsilon - \eta)}.
\]

By defining the generalized Fermi integrals as [31,33]

\[
a F_\varepsilon^m(\eta) = \int_0^{\infty} \left( -\frac{\partial f}{\partial \varepsilon} \right) \varepsilon^m(\varepsilon + \varepsilon^2\alpha)^m [(1 + 2\varepsilon\alpha)^2 + 2]^{1/2} d\varepsilon,
\]

the transport coefficients are expressed as follows:

The Seebeck coefficient:

\[
S = \frac{k_B}{e} \left[ \rho F_0^{1/2} - \eta \right].
\]

The carrier density, which is proportional to the effective density of states \( N_C \):

\[
p = N_C e^{0} F_0^{3/2} = \frac{(2m^*_L k_B T)^{3/2}}{3\pi^2 \hbar^3} e^{0} F_0^{3/2}.
\]

The mobility:

\[
\mu = \frac{e \langle \tau_{ac}(\varepsilon) \rangle}{m^*_c} = \frac{2\pi \hbar^2 e C_1}{m^*_c (2m^*_L k_B T)^{3/2}} E_d^{3/2} e^{0} F_0^{3/2},
\]

where \( k_B \) is the Boltzmann constant, \( \hbar \) is the reduced Planck’s constant, and \( e \) is the electronic charge. \( C_1 \) is the parameter determined by the combination of the elastic constants, and \( E_d \) is the deformation potential [4,31].

The Hall factor:

\[
A = \frac{3K (K + 2) e^{0} F_0^{1/2} e^{0} F_0^{3/2}}{(2K + 1)^2} \left( e^{0} F_0^{1/2} \right)^2.
\]
The Hall coefficient $R_H$ is related to the carrier density $p$ and the Hall factor $A$ through the equation:

$$R_H = A/ep.$$  

(9)

The masses $m^*_n$ and $m^*_p$ entered into the mobility expression are the density of states mass and the conductivity mass of a single ellipsoid, respectively, and both are related to the total density of states mass through [34]:

$$m^*_n = N^{-2/3}m^*_d$$  

(10)

and

$$m^*_p = m^*_dN^{-2/3}\frac{3K^{2/3}}{2K + 1},$$  

(11)

where $N$ is the number of the equivalent valleys and $K$ is the band anisotropy, defined previously.

B. Main electronic properties of PbSe

Previous papers on electrical, optical, and thermoelectric properties of both $n$- and $p$-type PbSe focused mainly on low temperatures and carrier densities and have shown similarities between the properties of $n$- and $p$-type PbSe [19–24,33,35–43]. The properties, however, deviate substantially at higher carrier concentrations and temperatures.

Transport and optical investigations on $n$-type PbSe have confirmed the nonparabolic dispersion law of the conduction band [33,35,37,40,44]. The number of equivalent valleys is $N = 4$, and the band anisotropy parameter $K$ lies in the range of 1.75–2 [36,37,45]. A room temperature value of $m^*_d \sim 0.27 m_o$ was found to fit the concentration dependent Seebeck coefficient (the Pisarenko plot) of $n$-type PbSe, assuming a single-band Kane model and its temperature dependence follows the power law $m^*_d \propto T^{0.5}$ [33]. The temperature dependence of Hall mobility of $n$-type PbSe reveals two slopes; up to $\sim 500$ K, a slope of $\sim -2$ was observed, indicating band nonparabolicity, while for higher temperatures, an increased slope of $\sim -3$ was associated with possible optical phonons excitations [37]. The value of 25 eV was proposed for the effective deformation potential coefficient at room temperature after the analysis of the temperature dependent transport properties of $n$-type PbSe within the framework of the Kane model and the assumption of acoustic phonon scattering [33].

As with $n$-type samples, the room temperature Pisarenko plot of $p$-type PbSe was fitted by the incorporation of a single-band model and the room temperature effective mass for the $L$ point maximum was found $m^*_dL \sim 0.27 - 0.28 m_o$. Similar effective masses were obtained by the assumption of either a single nonparabolic [19] or single parabolic band model [24]. However, discrepancies were observed concerning the carrier density regime at which the agreement between the theoretical and the experimental behavior was achieved [19,24]. The analysis of the temperature dependent thermopower in the framework of a single-band Kane model has shown that up to $\sim 450$ K, the power law of $m^*_dL \propto T^{0.5-0.8}$ was found to hold, while for higher temperatures a strong rise of the effective mass was observed [19]. Two slopes were also observed in the temperature dependence of the Hall mobility; up to $\sim 500$ K, the mobility scales with the temperature following $\mu \propto T^{-(1.5-2.8)}$, while for higher temperatures, it scales according to $\mu \propto T^{-(4.2-4.6)}$ [19]. Pei et al. [2] assumed that a higher deformation potential coefficient, i.e., 35 eV, of the $L$ point valence band might be responsible for the lower room temperature mobility of the $p$-type compositions relative to the respective $n$-type ones. Additionally, the comparison between $n$- and $p$-type PbSe with carrier densities in the range of $1 \times 10^{20} \text{cm}^{-3}$ has shown that the Seebeck coefficient is comparable up to $\sim 450$ K, with the $n$-type showing considerably lower values at higher temperatures [24].

The above papers indicate that at relatively low carrier densities and temperatures, the behavior of the transport properties of $p$-type PbSe may be explained satisfactorily by a single-band model resembling those of $n$-type analog [2,33]. The significant deviations from the single-band behavior observed at high carrier densities and temperatures actually demonstrate the necessity for the presence of an additional extremum located deeper in the valence band. The presence of the second hole band is supported by the temperature dependent Hall coefficient, suggesting the conduction of two types of carriers [21]. At sufficiently high doping and temperature, this second extremum dominates the transport properties of $p$-type PbSe.

A simplified depiction of the band structure of PbSe is shown in Fig. 1(a). Two symmetric bands at the $L$ point of the Brillouin zone separated by a direct energy gap $E_g$, and a second valence band located at the $\Sigma$ point with a valence band offset $\Delta E$ are assumed. The $L$ point valence band with degeneracy $N_{VL} = 4$ is denoted as the light-hole band and the highly degenerate $\Sigma$ point valence band with $N_{V\Sigma} = 12$ [2,22] as the heavy-hole band. Theoretical calculations based on the generalized gradient approximation (GGA) have shown a flat, high mass band at $\sim 0.35$ eV (0 K) below the band edge [26], while the quasiparticle self-consistent GW (QS GW) approach point to a secondary band maximum between the $\Gamma$ and $X$ points of the Brillouin zone [46]. The room temperature direct gap is $\sim 0.26$ eV [47,48], and the valence band offset is valued $\sim 0.25$ eV [21]. As it is shown in Fig. 1(b) on raising
temperature, the direct gap increases with a rate of \(\sim 10^{-4} \text{ eV/K}\) [9,49] and the light-hole band moves downwards, resulting in the decrease of the valence band offset and in band convergence at \(\sim 1500\) K [21]. Recent spectroscopic studies (angle-resolved photoemission spectroscopy [ARPES]) of the electronic band structure of PbSe revealed an unusual temperature dependent relationship between the valence band maxima and a band convergence at \(\sim 1300\) K [50]. The convergence of the these valence bands and the increase in the effective valley degeneracy at higher temperatures through the appearance of the heavy-hole band on the Fermi surface is believed to be the reason for the deviation from the single-band model behavior reported above and for the unique thermoelectric properties of \(p\)-type PbSe.

To extract the “hidden” transport coefficients of the heavy-hole band and their temperature dependence, we analyzed the experimental transport properties of heavily doped \(p\)-type PbSe in the framework of the two-band model, as illustrated in Fig. 1(a). The material parameters used for modeling the experimental data is summarized in Table I. For the temperature dependent \(L\) point direct gap [see Fig. 1(b)], we used the experimental values obtained by diffuse reflectance spectroscopy measurements on PbSe [9,48]. The relative position of the two inequivalent valence band maxima of Figs. 1(a) and 1(b) was obtained from the analysis of the temperature dependent absorption coefficient of doped PbSe after the subtraction of the free-carrier contribution [9,21].

The effective mass of the light-hole band was assumed to follow the same temperature dependence obtained for \(n\)-type PbSe [33]. The band degeneracy values of 4 and 12 were assumed for the light- and heavy-hole bands, respectively [2,22]. Similar to \(n\)-type PbSe, the light-hole band is assumed nonparabolic and anisotropic with a temperature independent anisotropy factor \(K\) of 1.75 [33,36,37], where the heavy-hole band is taken, for simplicity, as parabolic and isotropic. The elastic constants were taken to be temperature independent and equal to 9 GPa [31].

### C. The two-band model

In the presence of two bands, the total transport coefficients are determined by the transport coefficients of the individual components. The transport coefficients of the light-hole band were calculated from Eqs. (4)–(11). The corresponding coefficients of the heavy-hole band were obtained by the respective equations of the \(L\) band, accounting for the parabolic dispersion law by setting \(a = 0\) in Eq. (4) and writing the reduced chemical potential as \(\eta_{\Sigma} = \eta_L - \Delta E/k_BT\), where \(\Delta E\) is the valence band offset defined in Fig. 1(a).

For two-band semiconductors, the total Seebeck and Hall coefficients from both bands is given [13,51]

\[
S = \frac{S_L \sigma_L + S_{\Sigma} \sigma_{\Sigma}}{\sigma_L + \sigma_{\Sigma}} = \frac{S_L f + S_{\Sigma}}{f + 1} \tag{12}
\]

\[
R_H = \frac{R_{HL} \sigma_L^2 + R_{\Sigma} \sigma_{\Sigma}^2}{(\sigma_L + \sigma_{\Sigma})^2} = \frac{R_{HL} f^2 + R_{\Sigma}}{(f + 1)^2}, \tag{13}
\]

where \(\sigma_L, \sigma_{\Sigma}\) are the partial electrical conductivities, \(S_L\) and \(S_{\Sigma}\) are the partial Seebeck coefficients, and \(R_{HL}\) and \(R_{\Sigma}\) are the partial Hall coefficients. The parameter \(f\) accounting for the conductivity ratio is given by [13]

\[
f = \frac{f_0}{\eta_{\Sigma} \rho_{\Sigma} F_{\Sigma}(\eta_{\Sigma}, 0)} \tag{14}
\]

where the constant \(f_0\) is proportional to the ratio of the relaxation times and the effective masses of the two bands [13].

For the analysis of the room temperature Pisarenko plot, the above equations are simplified by using the relation \(\sigma_i = e \rho_i \mu_i\) and defining a constant mobility ratio \(b = \mu_L/\mu_{\Sigma}\)

\[
S = \frac{S_L \rho_L b + S_{\Sigma} \rho_{\Sigma}}{\rho_L + \rho_{\Sigma}}, \tag{16}
\]

\[
R_H = \frac{A_L \rho_L b^2 + A_{\Sigma} \rho_{\Sigma}}{e (\rho_L b + \rho_{\Sigma})^2}, \tag{17}
\]

where \(\rho_L, \rho_{\Sigma}\) and \(A_L, A_{\Sigma}\) are the partial hole densities and Hall factors of the \(L\) and \(\Sigma\) bands, respectively [4,15,52].

### II. EXPERIMENTAL

Ingots with nominal compositions \(\text{Pb}_{1-x}\text{Na}_x\text{Se}\) (0 \(\leq x \leq 0.04\)) were prepared by mixing appropriate ratios of reagents into carbon-coated quartz tubes. The tubes were sealed under vacuum (\(\sim 10^{-4}\) Torr), heated to 1150 °C over a period of 12 h, soaked at that temperature for 5 h, slowly cooled to...
than a single-band model is the most appropriate. Our results
pestle to reduce the particle size
processed. They were ground by a mechanical mortar and
over 3 h. Compositions with 0
ph
Composition
PbSe (ingot) 0.23 226.3 1295 483
Pb0.99Na0.01Se (−//−) 1.15 98.8 986 1854
Pb0.99Na0.003Se (−//−) 2.11 75.7 765 2583
Pb0.99Na0.004Se (−//−) 3.29 48.4 553 2912
Pb0.98Na0.005Se (ingot/SPS) 5.74/6.02 52.5/44.5 314/224 2889/2155
Pb0.9925Na0.0075Se (−//−) 7.33/11.6 30.3/29.5 247/146 2903/2720
Pb0.9915Na0.0085Se (SPS) 15.3 31.7 116 2840
Pb0.96Na0.04Se (ingot) 10.7/16 28.9/28.6 170/116 2922/2981
Pb0.96Na0.02Se (−//−) 25.1/34.8 21.8/21.9 82/51 3264/2861
Pb0.97Na0.01Se (−//−) 45.0/52.1 22.4/25.6 52/38 3726/3159
Pb0.96Na0.02Se (ingot) 61.8 26.07 26 2606

Table II. Room temperature hole density \( (p_h = 1/R_H) \), Seebeck coefficient \( (S) \), Hall mobility \( (\mu_H) \), and electrical conductivity \( (\sigma) \) of Pb\(_{1-x}\)Na\(_x\)Se compositions. The last column is the chemical potential \( (\eta) \) obtained after fitting the room temperature Pisarenko plot.

### III. RESULTS AND DISCUSSION

Before proceeding to the application of the two-band model, we address that the assumption of a Kane-type light-hole band is actually based on the room temperature concentration dependence of the Hall mobility (see Table II) [2,19,33]. We found that the consideration of a nonparabolic light-hole band using Eqs. (6)–(9) predicts better the experimental results (not shown) compared to a parabolic one [33]. The necessity for a lower lying secondary heavy-hole band was confirmed by the application of the single nonparabolic band model to the temperature dependent transport properties using Eqs. (5) and (9). The obtained temperature and concentration dependences of the effective mass in conjunction with the anomalous temperature dependence of the experimental Hall coefficient [15,18,19,21,53] indicated that a two-band rather than a single-band model is the most appropriate. Our results within the framework of a single-band model were found in good agreement with already published ones [2,19,24,33].

**A. Room temperature Pisarenko plot and hole density distribution in the two valence bands**

To determine the effective mass of the heavy-hole band, we analyzed the data on the room temperature Pisarenko plot; see Fig. 3(a). Table II summarizes the Hall density and the Seebeck coefficient of the Pb\(_{1-x}\)Na\(_x\)Se compositions used to construct the \( S \) versus \( p_h \) plot. As can be seen from Table II, the \( x \) values cover a wide range, 0 \( \leq x \leq 0.04 \), and the final compositions yield hole densities in the range \( \sim2 \times 10^{18} – 6 \times 10^{20} \text{ cm}^{-3} \). Both polycrystalline ingots and SPS-processed samples were used. Differences are observed between ingots and SPS samples concerning the hole density for the same amount of Na doping.

In Fig. 2, we compare the measured carrier concentrations together with the theoretical values obtained by the assumption that each substitutional Na atom creates one hole. It is clear from Fig. 2 that the best agreement between experimental and calculated hole densities is found for the SPS samples. The systematic deviation of the ingots’ values is attributed to the incomplete solubility as a result of partial Na

![FIG. 2. (Color online) Comparison of the room temperature hole density \( (p_h = 1/R_H) \) of the ingots and SPS processed Pb\(_{1-x}\)Na\(_x\)Se compositions against Na content. The dashed line indicates the theoretical hole density obtained by the assumption that each Na atom creates one hole.](image-url)
The heavy-hole band at room temperature is still ambiguous. Pisarenko plot at
firm the complex nature of the valence band structure of
settled. Despite these similarities, the PbSe case is not completely
than 2
PbTe. For
was found to be true for both K-doped [39] and Na-doped PbTe.
responsible for the saturation of the Seebeck coefficient. This
behavior: (a) it drops from
\( V / K \) when the carrier concentration is
\( \times 10^{20} \text{ cm}^{-3} \). The Seebeck coefficient, shown as a blue line in Fig. 3(a), was calculated using an
effective mass \( m^*_{lh} = 0.27 m_o \) for the light-hole band. This value of \( m^* \) is in good agreement with the one proposed by
et al. [33] and Vinogradova et al. [19] after the Pisarenko analysis of Na-doped PbSe samples considering a single-band model and acoustic phonon scattering. An effective mass of
is found to fit the Pisarenko relation in the low hole density limit in the case of K-doped PbSe [39].

Figure 3(a) shows the experimental Seebeck coefficients as a function of the Hall carrier density at room temperature. As can be seen, the measured Seebeck coefficient shows dual behavior: (a) it drops from \( \sim 230 \text{ \mu V/K} \) for the lightly doped compositions to \( \sim 30 \text{ \mu V/K} \), as the hole density reaches the value of \( \sim 1 \times 10^{20} \text{ cm}^{-3} \) and (b) saturates at around 26 – 29 \( \text{\mu V/K} \) when the carrier concentration is > \( 1 \times 10^{20} \text{ cm}^{-3} \).

This situation is similar to the one observed in p-type PbTe [4,14,56,57]. For p-type PbTe, the flattening of the Pisarenko plot at \( \sim 50 \text{ \mu V/K} \) for hole densities greater than \( \sim 5 \times 10^{19} \text{ cm}^{-3} \) was explained by a two-band model of a light- and a heavy-hole band. It was established that at low hole densities, the light mass band dominates the thermopower, while at high hole densities, as the Fermi level moves deeper into the valence band, the heavy band contribution is responsible for the saturation of the Seebeck coefficient. This was found to be true for both K-doped [39] and Na-doped PbTe. Despite these similarities, the PbSe case is not completely settled.

Although both theoretical and experimental studies confirm the complex nature of the valence band structure of PbSe [21,50,58], the picture concerning the contribution of the heavy-hole band at room temperature is still ambiguous. Wang et al., based on the Pisarenko plot of Na-doped PbSe [9,24], suggested that the contribution is negligible up to hole densities \( \sim 3 \times 10^{20} \text{ cm}^{-3} \), and a single-band model was found to explain well their experimental data. Zhang et al. [39] proposed that in the case of K-doped PbSe up to \( \sim 1.5 \times 10^{20} \text{ cm}^{-3} \), the main contribution comes from the light-hole band, while Vinogradova et al. [19] stressed the deviation from a single-band model for hole densities higher than \( 2 \times 10^{20} \text{ cm}^{-3} \).

In this paper, we studied compositions with very high hole densities, reaching the values of \( \sim 6 \times 10^{20} \text{ cm}^{-3} \) (see Table II). Since the saturation of the thermopower for hole densities \( \sim 6 \times 10^{20} \text{ cm}^{-3} \) is an experimental fact, we conclude that for the heavily doped p-type PbSe compositions, the heavy-hole band does contribute to the transport even at room temperature. Using Eqs. (16) and (17), we performed the analysis and calculated the room temperature effective masses of the two bands, the partial Seebeck coefficients, and the partial hole densities as a function of hole doping.

The parameters of the L band were determined by employing the single Kane model and Eq. (5), and adjusting the density of states mass to obtain the best fit to the experimental values up to Hall densities \( \sim 1 \times 10^{20} \text{ cm}^{-3} \). The Seebeck coefficient, shown as a blue line in Fig. 3(a), was calculated using an effective mass \( m^*_{lh} = 0.27 m_o \) for the light-hole band. This value of \( m^* \) is in good agreement with the one proposed by Wang et al. [33] and Vinogradova et al. [19] after the Pisarenko analysis of Na-doped PbSe samples considering a single-band model and acoustic phonon scattering. An effective mass of
was found to satisfy the Pisarenko relation in the low hole density limit in the case of K-doped PbSe [39].

In Fig. 3(a), we also plot the concentration dependent Seebeck coefficient for several n-type PbSe compositions. Considering the PbCl_2-doped materials [37], the experimental values are in fairly good agreement with the theoretical ones, suggesting that the effective mass, \( m^*_{lh} = 0.27 m_o \), is the same for the conduction and the light-hole valence bands of PbSe. A similar conclusion was reached by Wang et al. after the comparison of Br-doped PbSe with the p-type analogs up to \( 1 \times 10^{20} \text{ cm}^{-3} \) [33]. Accordingly, Chernik et al. [59] suggested that the conduction and the valence bands of PbSe have similar parameters up hole densities of \( \sim 1 \times 10^{20} \text{ cm}^{-3} \).

The last column of Table II tabulates the chemical potential values obtained by the fitting of the Pisarenko plot with the single Kane model. As can be seen, the chemical potential increases with Na amount and moves from the L point band edge for the undoped PbSe to \( \sim 0.33 \text{ eV} \) deeper in the valence band when the hole density reaches \( \sim 6 \times 10^{20} \text{ cm}^{-3} \). With the density of states mass of the L band at \( 0.27 m_o \), there are three adjustable parameters that define the total Seebeck coefficient [Eqs. (16) and (17)], namely, the energy difference between the two branches, \( \Delta E \), the heavy-hole band effective mass, and the mobility ratio of the two subbands.

Starting with the valence band offset \( \Delta E \), the room temperature value of \( \sim 0.25 \text{ eV} \) was proposed based on the absorption coefficient spectra of hole-doped PbSe (see Table I) [21,22]. To confirm this value, we followed the analysis performed by Kolomoets et al. for p-type PbTe [13]. Assuming a single-band model, we calculated the density of states mass for each of our compositions using the Eqs. (5) and (6). We observe that up to \( \sim 1 \times 2 \times 10^{20} \text{ cm}^{-3} \) the obtained effective mass is almost constant \( \sim 0.23 \sim 0.27 m_o \), while for higher hole densities, there is an abrupt increase. This increase of the effective mass actually denotes the failure of the single-band model due to the contribution of the high mass heavy-hole band. According to Kolomoets et al. [13], the value of the chemical potential at the knee point of the dependence of the effective mass on carrier density is actually the room temperature valence band offset. As can be seen from Table II, the chemical
potential is $-0.21 - 0.25$ eV for hole densities in the range $1 - 2 \times 10^{20} \text{cm}^{-3}$ (at the knee point of the dependence of the effective mass on carrier density) quite close to the valence band offset predicted by the respective equation of Table I. At the same range of hole densities, the Seebeck coefficient saturates [see Fig. 3(a)], meaning that the chemical potential at the onset of the flattening of the Pisarenko line is essentially the band offset for a two-band model.

Concerning the density of states mass of the heavy-hole band, different values have been proposed in the literature. Based on optical investigations of $p$-type PbSe, Veis et al. [22] proposed the value $\sim 2.5 m_o$, while the same value was found to describe the flattening of the Pisarenko plot of the $Kp$, $\text{Pb}_{1-x}, \text{Se}$ at high hole densities [39]. Gurieva et al. [23] have adopted a value of $\sim 2 m_o$ to describe the temperature dependence of the Hall coefficient of $p$-type PbSe. Theoretical calculations of the band structure of PbSe yielded an average mass $\sim 0.48 m_o$ for one ellipsoid [46], which based on Eq. (10) and assuming a band degeneracy of 12, gives the total effective mass the value of $\sim 2.5 m_o$. On the other hand, Veis et al. [21], based on the temperature dependent Hall coefficient, and Wang et al. [9], after modeling the high temperature transport coefficients of $\text{Pb}_{1-x}, \text{Sr}, \text{Se}$ on the assumption of a mixed scattering mechanism, suggested a room temperature value of $\sim 4.5 m_o$.

The determination of the heavy-hole band effective mass from the best fitted Seebeck data in the concentration range where the Pisarenko plot flattens [Fig. 3(a)] was found to be more challenging, because the total Seebeck is codetermined by the heavy-hole effective mass and the mobility ratio, in a way that the best fit yields higher effective mass for higher mobility ratio. However, as we shall show later, the temperature dependent transport properties are well described by adopting the value of $\sim 2.5 m_o$ for the heavy-hole band, in accordance with Veis et al. [22] and Zhang et al. [39]. Consequently, the best fit to the experimental data using the total Seebeck coefficient, i.e., the black line in Fig. 2(a), was obtained by adjusting the room temperature mobility ratio $b$ to the value of $\sim 4$. The dashed red line of Fig. 3(a) shows the concentration dependent thermopower of the heavy-hole band, as obtained from the two-band model. The Seebeck coefficient of the $\Sigma$ band is higher than that of the $L$ band over the whole concentration range, owing to the higher effective mass. As expected, the total Seebeck is a weighted average of the individual bands and lies closer to the Seebeck values of the $L$ band.

Based on the fitting of the Pisarenko plot, Fig. 3(b) displays the room temperature relative population of the individual bands as obtained by the partial hole densities. As can be seen, the fraction of holes in the light-hole band is almost unity up to a critical concentration of $\sim 1 \times 10^{20} \text{cm}^{-3}$. Up to this concentration range, the Seebeck coefficient of Fig. 3(a) matches a Pisarenko relation calculated from the parameters of the light-hole band alone [the blue line of Fig. 3(a)], while for higher hole densities, the thermopower starts to saturate. Based on these observations, the critical $L$ band population may be assumed to be $\sim 1 \times 10^{20} \text{cm}^{-3}$ holes, since up to these hole densities, the $\Sigma$ band may be considered to be almost empty. For higher hole densities, the chemical potential (see Table II) moves deeper in the valence band, and the heavy-hole band starts to acquire a steady fraction of holes.

For $2 \times 10^{20} \text{cm}^{-3}$ holes, the chemical potential crosses the band edge of the $\Sigma$ band, $\eta = \Delta E$, and for $6 \times 10^{20} \text{cm}^{-3}$ holes, the chemical potential is located below the heavy-hole band edge, $\eta = 0.33 \text{eV}$ (Table II). These findings actually demonstrate why the heavy doping is necessary to probe the high density of states heavy-hole band in PbSe.

The room temperature saturation thermopower for $p$-type PbTe was found around $50 \mu \text{V/K}$, and the Pisarenko analysis based on a two-band model suggested only $\sim 5 \times 10^{19} \text{cm}^{-3}$ holes are sufficient for the Fermi level to reach the $\Sigma$ band maximum [14,17]. This difference in the light-hole band population between PbTe and PbSe arises from the lower $L/\Sigma$ energy offset in PbTe [17].

### B. Partial transport coefficients

After the determination of the room temperature parameters, we extended the application of the two-band model to higher temperatures to describe the temperature dependence of the transport coefficients of the three heavily doped $\text{Pb}_{1-x}, \text{Na}, \text{Se}$ compositions with $x = 0.01, 0.02,$ and $0.03$. The measured temperature dependent Seebeck coefficients, electrical conductivities, and Hall coefficients are displayed in Fig. 4. The experimental Seebeck coefficients show typical behavior of degenerate semiconductors and increase with the temperature [Fig. 4(a)]. All the samples show comparable room temperature values $\sim 25 \mu \text{V/K}$, while for higher temperatures, the thermopower scales with the Na amount. For the $x = 0.01$
FIG. 5. (Color online) (a) The Fermi level as a function of temperature obtained by the application of the two-band model for the $x = 0.01$, 0.02, and 0.03 compositions, (b) the Fermi level relative to the position of the light-hole and the heavy-hole valence bands. Composition, the Seebeck coefficient reaches $\sim 200 \mu V/K$ at 900 K, while the $x = 0.02$ and $x = 0.03$ compositions show $\sim 170$ and $\sim 160 \mu V/K$, respectively. The room temperature electrical conductivities are high $\sim 2900$–$3100 S/cm$. The conductivity decreases with increasing temperature and has higher values with higher Na amounts over most of the temperature range [Fig. 4(b)]. The temperature dependent Hall coefficients, $R_H$, [Fig. 4(c)] show typical two-band behavior [4,15,53]. Up to $\sim 300 K$, the Hall coefficient is almost constant; for higher temperatures it increases reaching a maximum at $\sim 650 K$ and then decreases. The experimental values scale with the Na content in the whole temperature range, i.e., higher Na amount yields lower Hall coefficient. Using the low temperature values, we obtained the apparent hole densities ($p = 1/R_{H10K}$) for the $x = 0.01$, 0.02 and 0.03 samples, i.e., $\sim 1.8 \times 10^{20}$, $4.7 \times 10^{20}$ and $7.6 \times 10^{20} cm^{-3}$ respectively.

The application of the two-band model requires knowledge of the temperature dependences of all parameters involved in the calculations. Those are summarized in Table I. The fitting was performed to the experimental transport coefficients of Fig. 4 using the Eqs. (12)–(15). The reduced chemical potential and the conductivity ratio $\delta_0$ were adjusted to fit the temperature dependent Seebeck and Hall coefficients. The studied compositions are extrinsic heavily doped semiconductors with no sign of bipolar contribution. Thus, the analysis assumes that at each temperature the neutrality condition holds in the form [13,18,57]:

$$p = p_L + p_S = \text{const.}$$

where $p$ is the apparent hole density obtained by the low temperature Hall coefficient ($p = 1/R_{H10K}$).

The results of our analysis are displayed in Figs. 5–7. For each composition, the temperature dependent chemical potential (Fermi levels, $\eta$) and their relative position within that valence band structure are summarized in Figs. 5(a) and 5(b), respectively. The partial transport coefficients of the two valence bands are included as red and blue lines—symbols and the best fit total Seebeck and Hall coefficients are denoted as black solid lines in Figs. 6 and 7.

We start our discussion with the best fit obtained chemical potential values of Fig. 5(a). In this way, we can illustrate the effect of doping and the temperature on the extracted transport coefficients of the two valence bands. The room temperature chemical potentials ($\eta$ values) of the studied compositions are in the range of $\sim 0.2$–$0.35 eV$ and in good agreement with the respective values listed in Table II. The small discrepancies observed are attributed to the fact that the $\eta$ values of Table II are obtained using the room temperature Hall coefficient, while those of Fig. 5 (a) are obtained using the Hall coefficient at $T \sim 50 K$. The conductivity ratio $\delta_0$ as a function of temperature for the three studied materials. Note that for $T \sim 650 K$ the conductivity ratio convergences to unity.
∼10 K with the ratio $R_{H^0/0}/R_{H^0/0} ∼ 1.12$. On raising the temperature to 900 K, the chemical potential decreases. For the $x = 0.01$ composition, $\eta$ is almost zero at 900 K, while for the $x = 0.02$ and 0.03 samples $\sim 0.15$ eV. The two most heavily doped compositions show a sharper decrease of the chemical potential in the whole temperature range relative to the $x = 0.01$ sample. For the latter, a slightly different slope is observed for temperatures higher than ∼500 K.

In Fig. 5(b), we present the relative position of the chemical potentials obtained after subtracting the $\eta$ values from the line that represents the position of the light-hole band. It is clear that for the $x = 0.01$ sample the chemical potential lies higher in energy than the heavy-hole band maximum in the whole temperature range. However, the difference between the two levels is in the range of $1.6 - 1.2 k_B T$ in going from 300 to 900 K. For the $x = 0.02$ and 0.03 samples, the chemical potential is lower than the heavy-hole band at room temperature. At ∼600 K, the Fermi level is crossing the heavy-hole band for the $x = 0.02$ composition and for the $x = 0.03$ the crossing is observed at ∼900 K.

Figures 6(a)–6(c) display the partial Seebeck dependence of the partial hole densities for the $x = 0.01, 0.02$, and 0.03 samples. As can be seen, with increasing temperature, there is a monotonic reduction of the light-hole band carrier density following the decrease of the chemical potential. This gives rise to the corresponding increase of the heavy-hole band carrier concentration as a result of the neutrality condition. The rate of the carrier’s density variation is proportional to the valence band offset reduction, i.e., $10^{-3}$ cm$^{-3}$/K. For the $x = 0.01$ composition [Fig. 6(a)], the room temperature hole densities for the two valence bands are $\sim 1.6 \times 10^{20}$ and $\sim 1 \times 10^{19}$ cm$^{-3}$, and the light-hole band is expected to contribute most. At higher temperatures, holes are excited to the heavy-hole band, so at ∼800 K, both bands show the same number of holes $\sim 8 \times 10^{19}$ cm$^{-3}$. For the $x = 0.02$, the hole densities are $\sim 3 \times 10^{20}$ and $1.5 \times 10^{20}$ cm$^{-3}$ for the light- and heavy-hole band, respectively. The equality in hole population is now observed at ∼500 K [Fig. 6(b)]. The room temperature chemical potential value for the $x = 0.03$ sample [Fig. 5(a)] is found $\sim 0.32$ eV, and both of the bands show comparable population of $\sim 3 - 4 \times 10^{20}$ cm$^{-3}$ [Fig. 6(c)]. For this composition, the crossing of the hole densities is at ∼400 K and the heavy-hole band carrier density at 900 K is $\sim 5.5 \times 10^{20}$ cm$^{-3}$. The major points from Figs. 5 and 6(a)–6(c) are (i) the position of the chemical potential is lowered as a result of hole doping in the whole temperature range, (ii) at high temperatures, the chemical potential moves to the band gap, and holes are transferred from the light- to heavy-hole band, and (iii) the crossing point where holes exist in both bands is concentration dependent and shifts from ∼800 to ∼400 K, when the total hole density increases from $\sim 2 \times 10^{20}$ (x = 0.01) to $\sim 8 \times 10^{20}$ cm$^{-3}$ (x = 0.03), respectively.

Figures 6(d)–6(f) display the partial Seebeck coefficients and the calculated thermopower for the best two-band model fit for each sample composition. As can be seen, the agreement between the model and the experimental values is good in the whole temperature range. Considering first the $x = 0.01$ composition of Fig. 6(d), the experimental Seebeck follows very close the calculated Seebeck coefficient of the light-hole band up to ∼500 K. The slope of the experimental Seebeck coefficient changes slightly at ∼600 K. For higher temperatures, the experimental thermopower is larger than that of the light-hole band, suggesting that the $\Sigma$ band contribution is restricted mainly to temperatures higher than ∼500 K. On raising the temperature to 900 K, the $L$ band thermopower changes from ∼30 to 160 $\mu$V/K, while that of the $\Sigma$ band decreases from ∼350 $\mu$V/K and saturates at ∼300 $\mu$V/K at high temperatures. The decrease of the reduced chemical potential [Fig. 5(a)] gives rise to the increase of the light-hole band thermopower with rising temperature. The saturation of the heavy-hole band Seebeck is the result of the variation of the respective chemical potential $\eta_\Sigma$. The latter is found negative in the whole temperature range and is nearly saturated for temperatures higher than ∼500 K.

For the two most heavily doped compositions $x = 0.02$ and 0.03, the situation is different [Figs. 6(e) and 6(f)] relative to the $x = 0.01$ sample discussed above. Here, the change of the slope of the experimental $S$ vs. $T$ plot is clearly more pronounced. The Seebeck coefficient of the $L$ band is lower than the measured ones in the whole temperature range. For these samples, the contribution of the heavy-hole band is pronounced even at room temperature, where the chemical potential is lower than the heavy-hole band edge [Fig. 5(a)]. This explains the Pisarenko plot of Fig. 3(a), where Seebeck flattening for hole densities beyond $\sim 2 \times 10^{20}$ cm$^{-3}$ is observed. For both of these samples, the carrier density of the heavy-hole band at room temperature is higher than $1 \times 10^{20}$ cm$^{-3}$ [Figs. 6(b) and 6(c)]. For the $x = 0.02$, composition the Seebeck coefficient of the light-hole band varies from $\sim 10 - 120 \mu$V/K, while for the $x = 0.03$ composition from $\sim 80 - 100 \mu$V/K. In each case, the heavy-hole band displays increasing Seebeck values with rising temperature, suggesting a nearly degenerate band. For the $x = 0.02$ sample, the thermopower varies from $\sim 150 - 230 \mu$V/K, while for the $x = 0.03$, changes from $\sim 100 - 200 \mu$V/K.

Our results on the partial Seebeck coefficients clearly demonstrate the effect of the complex valence band structure on the thermopower of PbSe. The contribution of the high mass-high Seebeck secondary band produces significantly higher Seebeck values of the $p$-type compositions relative to the $n$-type analogs discussed above. For doping levels up to $\sim 1.5 \times 10^{20}$ cm$^{-3}$ holes, the heavy-hole band is found underpopulated, considering its high density of states, and shows nearly constant Seebeck values $\sim 300 \mu$V/K above 600 K. Under heavy doping conditions, $> 4 \times 10^{20}$ cm$^{-3}$ holes, the behavior of the heavy-hole band resembles that of a nearly degenerate one displaying increasing Seebeck values with temperature. Due to the increased effective density of states, the heavy-hole band reaches $\sim 200 \mu$V/K for a population $\sim 5 \times 10^{20}$ cm$^{-3}$ holes at 900 K, when the light-hole band shows $\sim 100 \mu$V/K for $\sim 2 \times 10^{20}$ cm$^{-3}$ holes [Fig. 6(e)]. In general, the total Seebeck coefficient is expected to lie between the partial Seebeck coefficients of the two bands. Figures 6(d)–6(e) demonstrate that depending on doping level, the thermopower values as high as $\sim 250 \mu$V/K are expected at 1000 K. Additionally, it is now clear that decreasing the valence band offset one can decrease the temperature in which the heavy-hole band begins to contribute [9,12].
The comparison between the calculated and the experimental Hall coefficients is shown in Figs. 7(a)–7(c). In each case, the agreement is found to be good. At this point, we need to stress that a temperature independent heavy-hole mass of $2.5 m_o$ was found adequate to fit all the transport coefficients for the $x = 0.01$ and $x = 0.02$ compositions. For the $x = 0.03$ sample, this assumption yielded a poor fit to the experimental Hall coefficient (the maximum at $\sim 650$ K could not be reproduced). For this reason, it was necessary to assume a temperature dependent heavy-hole effective mass, i.e., $d \ln m^*/d T = 0.3$. One reason for this dependence could be the complex nature and anisotropy of the heavy-hole band [46].

The redistribution of carriers between the two valence bands give rise to an anomalous temperature dependence of the Hall coefficients [Figs. 7(a)–7(c)] [5,18,21,38]. As we have already shown, holes are transferred from the light- to heavy-hole band as a result of shifting of the chemical potential with raising temperature. Up to $\sim 650$ K, the increase of the Hall coefficient is related to the decrease of the light-hole density and to the high mass-low mobility heavy holes which contribute to a small amount [4]. Figure 7(d) presents the energy independent term of the conductivity ratio, $f_0$ [see Eq. (14)] for the three studied compositions. As can be seen, $f_0$ decreases with rising temperature and scales with the amount of Na up to $\sim 500$ K. At $\sim 650$ K (maximum of the Hall coefficient), $f_0$ is almost unity for the three compositions. A further increase in temperature makes $f_0$ lower than unity, decreasing continuously and converge irrespective of the hole density.

IV. CONCLUDING REMARKS

We have presented a study of the transport properties of $p$-type PbSe thermoelectric material that shows that the complex valence band structure of the material has profound impact on the thermoelectric performance. The effects of the heavy doping, and temperature, on both the Seebeck coefficient and the Hall coefficient were determined in detail. We have shown that the experimental transport coefficients may be well described with two moving inequivalent band maxima; a light-hole band and a lower lying heavy-hole band. The room temperature Pisarenko plot was described by adopting a nonparabolic light-hole band with effective mass $\sim 0.27 m_o$ that contributes most up to $\sim 1 \times 10^{20}$ cm$^{-3}$ holes, and a parabolic heavy-hole band with an effective mass of $\sim 2.5 m_o$, responsible for the flattening of the Pisarenko plot for hole densities higher than $\sim 2 \times 10^{20}$ cm$^{-3}$. The valence band offset determined by the chemical potential at the saturation point of the Pisarenko plot was found $\sim 0.25$ eV. With raising the temperature, the effective mass of the Kane-type light-hole band increases, resembling the behavior of the $n$-type analog. The temperature dependent valence band offset demonstrated that the crossing of the two bands takes place at high temperatures $\sim 1500$ K. The relative movement of the two bands resulted in the transferring of holes from the light-hole band to the heavy-hole band, giving rise to an anomalous temperature dependent Hall coefficient peaked at $\sim 650$ K. The assumption of a parabolic heavy-hole band with a temperature independent effective mass seemed to hold up to $\sim 4.7 \times 10^{20}$ cm$^{-3}$ holes. For hole densities higher than $\sim 7 \times 10^{20}$ cm$^{-3}$, such an assumption yielded a poor fit and a temperature dependent effective mass was found to describe better the experimental results. This might be an indication of the possible complexity and anisotropy of the heavy-hole band. Our analysis yielded the partial transport coefficients of the two valence bands over the widest temperature range of 300–900 K. At 900 K, the heavy-hole band can reach Seebeck values as high as 200–300 $\mu$V/K, accounting for the high thermopower of $p$-type PbSe and the outstanding thermoelectric performance of the material. We strongly believe that the extracted temperature and concentration dependent partial transport coefficients may serve as a guide for future band structure engineering towards the design of optimized PbSe-based thermoelectric materials. Our paper demonstrates the general similarity of the temperature dependence of the valence band structures of PbSe and PbTe. However, the larger valence band offset of the selenium analog accounts for the significant distinction and the different performance of the two lead chalcogenides thermoelectrics.

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